



## IMPROVEMENT OF THE SEISMIC RESISTANCE FOR STEEL STRUCTURES WITH HYBRID CONTROL SYSTEM

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**Abstract-** The paper presents a steel structure using hybrid control to resist seismic resistance. Both semi-active controlled stiffness devices (CSD) and passive controlled fluid viscous dampers (VFD) are used to attain higher capability control forces. The paper uses four active control algorithms, including (Riccati Optimal Active Control Algorithm, Instantaneous Control with Displacement and Velocity Feedback, Instantaneous Optimal Active Closed-Loop Control Algorithm, and Pole Placement Algorithm) to control the CSD of the structure. In the numerical example, maximum control forces in VFD are employed with the help of industrial manufactures such as Taylor Company. A benchmark steel building is a 20-story steel structure designed for the SAC project for Los Angeles, California, to analyze the dynamic responses of the building controlled subjected to earthquake-induced motion. Also, the efficiency of reducing dynamic responses in the building equipped with combined devices is compared to the uncontrolled building, the structure with only passive VFD, and with semi-active CSD. Finally, in conclusion, we discuss some advantages of the hybrid control system for seismic resistance in Vietnam.

**Keywords-** Dynamics of Structures, Dampers, Passive Control, Semi-Active Control, Viscous Fluid Dampers, Controlled Stiffness Devices

### I. INTRODUCTION

Hybrid control has economic advantages compared to passive control and semi-active control. It is passive dissipators responsible for seismic resistance to a weak earthquake and semi-active devices in charge of resisting a strong earthquake. Consequently, energy for a structure to mitigate the dynamic responses of the structure is required reasonably. Mixing both a controlled stiffness device and a fluid viscous damper into one brace is {1} to employ the strong points of both VFD and CSD, {2} to utilize the force generated from both of them during motion, {3} to create a passive and semi-active controllable system simultaneously. Furthermore, derived from the study in the field of structural control involving buildings equipped with only viscous fluid dampers (VFD) [3] or only controlled stiffness devices (CSD) [5], CSDs can be rapidly semi-active controlled. However, their drawback is the capability of producing variable force while VFDs are challenging to create a semi-active system. Control forces generated by VFD or CSD depend on the motion of two adjacent stories. The internal features of the VFD involve the flow of compressible silicone oil through specially designed passages located in and around the piston head. As opposed to CSD, a passive viscous damper force generated by VFD at the  $i^{th}$  floor is given by [3]  $F_i^{VFD}(t) = C_i^{VFD} |\dot{x}_i(t) - \dot{x}_{i-1}(t)|^\alpha \text{sign}[\dot{x}_i(t) - \dot{x}_{i-1}(t)]$  (1), where  $C_i^{VFD}$  is the damping coefficient;  $\dot{x}_i(t)$  is the velocity at the  $i^{th}$  floor;  $\alpha$  is a predetermined exponent. Usually for seismic application  $\alpha \square 1$ , producing the linear response. Otherwise, the variable force developed by the semi-active controlled stiffness devices at the  $i^{th}$  floor is given by [5]:

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$$u_i^{CSD}(t) = u_i^M + F_i^C \quad (2), \text{ where } \begin{cases} u_i^M = C_i^M [x_i(t) - x_{i-1}(t) + x_i^{ctr}(t)] \\ F_i^C = n_c C_C \left\{ x_0 - [x_i(t) - x_{i-1}(t)] \right\} \left\{ \sqrt{\frac{a^2 + x_0^2}{4}} - 1 \right\} \end{cases} \text{ with } C_i^M \text{ and}$$

$C_C$  are the stiffness coefficients of the mainspring and the corrector, respectively;  $n_c$  is the number of stiffness correctors;  $x_i(t)$  is the displacement;  $x_i^{ctr}(t)$  is the displacement of the activating bar at  $i^{th}$  floors;  $x_0$  is the horizontal projection of the corrector in the unloaded state;  $a$  is the diameter of the internal cylinder.

Due to the properties of CSD, the displacement of the mainspring is an inelastic domain; therefore,  $x_i^{ctr}(t)$  must satisfy  $x_{limit,i}^c \leq x_i[k] - x_{i-1}[k] + x_i^{ctr}(t) \leq x_{limit,i}^t$  (3), where  $x_{limit,i}^c$  and  $x_{limit,i}^t$  are compression and tension elastic limit at the  $i^{th}$  floor, respectively. The value of  $C_i^M$ ,  $x_{limit,i}^c$  and  $x_{limit,i}^t$  are taken from manufactures of CSD. A semi-active controlled force of CSD depends on the magnitude of both main spring's stiffness coefficient and compression and tension limit. The force is quite low compared to a structure's control force needed. Unlike an active control, the control computer determines the displacement of activating bar to produce the semi-active force vector  $u_i^{CSD}(t)$ , instead of the active force vector  $\hat{u}_i(t)$ . The determination of  $x_i^{ctr}(t)$  is related to the feedback control law obtained from control algorithms. In this paper, four active control algorithms applied to calculate  $u_i^{CSD}(t)$  consist of Riccati Optimal Active Control Algorithm (ROAC), Pole Placement Algorithm (PPA), Instantaneous Control with Displacement, and Velocity Feedback (ICDVF), and Instantaneous Optimal Active Closed-Loop Control Algorithm (IOAC). Eventually, the system combines the forces produced by the semi-active CSD and the additional passive VFD at the  $i^{th}$  arbitrary floor:  $u_i(t) = F_i^{VFD}(t) + u_i^{CSD}(t)$  (4)

The smart structures are assumed {1} to be shear building so that each floor is modeled as a degree of freedom where the mass is concentrated at each floor, and the stiffness is provided by columns and {2} to be able to retain elastic and columns' linear behavior under the earthquake. From these assumptions, a  $n$ -story multi-bay shear building is associated with an  $n$ -story single-bay building as shown in Figure 1, and the stiffness coefficient at the  $i^{th}$  floor of the shear building ( $i=1, 2, \dots, n$ ) can be calculated with the following expression [2]

$$k_i = \sum_{\text{columns}} \frac{12EI_c}{H^3} \quad (5), \text{ where } E \text{ is Young's modulus, } I_c \text{ is the moment of inertia of the columns; } H \text{ is the length of one column at the } i^{th} \text{ floor.}$$

For the purpose of assessing the effectiveness of response reduction, a reliable model of a controllable structure attaching with the hybrid system of (VFD+CSD) is required to establish the differential equation of motion, subsequently an algorithm to solve this equation. The goal of numerical examples is to estimate the effectiveness in reducing dynamic responses of the benchmark 20-story structure simultaneously equipped with VFD and CSD. This result is compared to such a structure with no control, with only passive VFD, semi-active CSD, and with a classical solution which increases the columns' stiffness of a structure.

## II. A SMART STRUCTURE CONTROLLED WITH HYBRID CONTROL

### II.1. The governing differential equation of motion

Consider an  $n$ -story single-bay shear building structure subjected to lateral forces and seismic excitations equipped with  $r$  dampers (VFD+CSD) at particular floors as shown in Figure 1, and  $m_i$  is the mass;  $P_i(t)$  is the lateral force at the  $i^{th}$  floor;  $w(t)$  is the vector of the ground accelerations. From the free-body diagram depicted in Figure 2, the motion equation of such a smart structure under seismic excitations can be expressed in matrix form as

$$\mathbf{M}\ddot{\mathbf{x}} + \mathbf{C}\dot{\mathbf{x}} + \mathbf{K}\mathbf{x} = \mathbf{F}_d\mathbf{u} - \mathbf{M}\mathbf{r}\mathbf{w} \quad (6), \text{ where } \mathbf{M} = \begin{bmatrix} m_1 & 0 & 0 & 0 & 0 \\ 0 & \dots & 0 & 0 & 0 \\ 0 & 0 & m_i & 0 & 0 \\ 0 & 0 & 0 & \dots & 0 \\ 0 & 0 & 0 & 0 & m_n \end{bmatrix}, \quad \mathbf{K} = \begin{bmatrix} k_1 + k_2 & -k_2 & 0 & 0 & 0 \\ 0 & \dots & 0 & 0 & 0 \\ 0 & -k_i & k_i + k_{i+1} & -k_{i+1} & 0 \\ 0 & 0 & 0 & \dots & 0 \\ \text{sym} & 0 & 0 & -k_n & k_n \end{bmatrix} \text{ are}$$

the constant mass stiffness matrices, respectively; and  $\mathbf{C}$  is the coefficient damping matrix and is determined with the help of Rayleigh method [2];  $\mathbf{r} = [1 \dots 1 \dots 1]^T$ ;  $\mathbf{F}_d$  is the matrix indicating the position of (VFD+CSD);

$\mathbf{x} = [x_1 \dots x_i \dots x_n]^T$ ;  $\dot{\mathbf{x}} = \frac{d}{dt} \mathbf{x}$ ;  $\ddot{\mathbf{x}} = \frac{d^2}{dt^2} \mathbf{x}$  are the displacement, velocity, and acceleration vectors of time,

respectively;  $\mathbf{u}(t) = \{P_1(t) - u_1 + u_2, \dots, P_i(t) - u_j + u_{j+1}, \dots, P_n(t) - u_r\}^T$  is force vector of time, where  $u_j$  is the combined force provided by the (VFD+CSD) and calculated with (4) ( $j = 1, 2, \dots, r$ ).

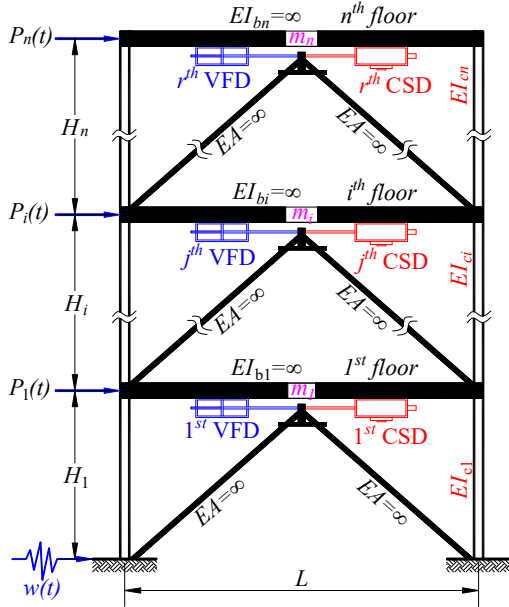


Figure 1. Multi-Story Building equipped with (VFD+CSD) modeled as shear building

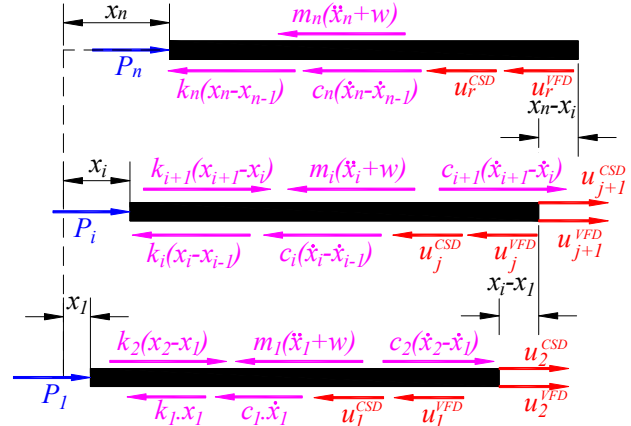


Figure 2. The free body diagram for structures with (VFD+CSD)

## 2.2. Feature of a structure with (VFD+CSD)

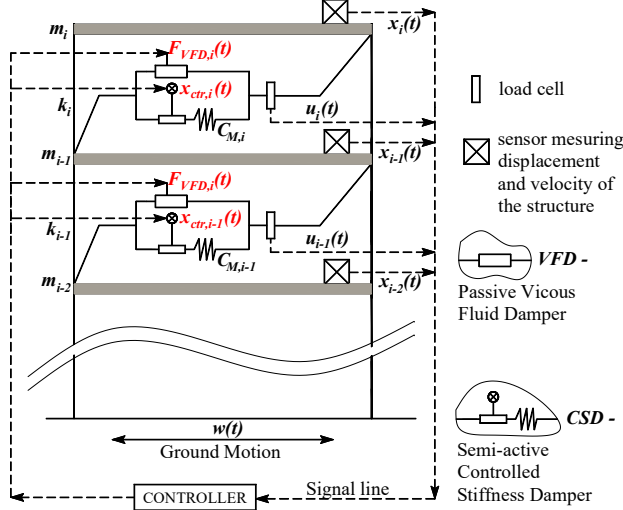


Figure 3. Schematic diagram of a structure with (VFD+CSD) and hybrid control system

Consider a seismic structure equipped with the multiple (VFD+CSD) as shown in Figure 3. For the hybrid structural system subjected to a seismic force, as shown in Figure 3, the motion of the system may be rewritten in a

state space equation:  $\dot{\mathbf{z}}(t) = \mathbf{A}\mathbf{z}(t) + \mathbf{B}\mathbf{u}(t) + \mathbf{E}w(t)$  (7), where the vector  $\mathbf{z}(t) = \begin{Bmatrix} \mathbf{x}(t) \\ \dot{\mathbf{x}}(t) \end{Bmatrix}$  represents the state of the

structure which contains the relative-to-ground velocities  $\dot{\mathbf{x}}(t)$  and displacements  $\mathbf{x}(t)$  of the structure;  $\dot{\mathbf{z}}(t) = \frac{d\mathbf{z}}{dt}$ ;

$\mathbf{A} = \begin{bmatrix} \mathbf{0} & \mathbf{I} \\ -\mathbf{M}^{-1}\mathbf{K} & -\mathbf{M}^{-1}\mathbf{C} \end{bmatrix}$  denotes the system matrix composed of the structural mass, damping and stiffness

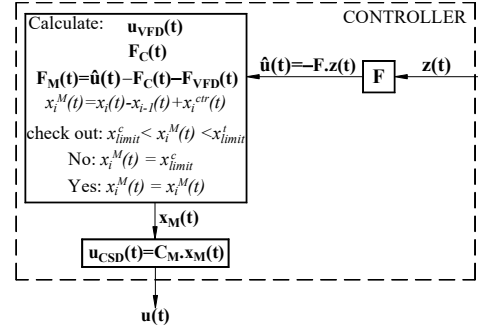


Figure 4. Controller block

matrices;  $\mathbf{B} = \begin{bmatrix} \mathbf{0} \\ \mathbf{M}^{-1} \cdot \mathbf{F}_d \end{bmatrix}$  is the distribution matrices of the control forces;  $\mathbf{E} = \begin{bmatrix} \mathbf{0} \\ -\ddot{r} \\ -\dot{r} \end{bmatrix}$  is the seismic excitations. The

responses of a structure with a hybrid control system are determined with the help of {1} the algorithm zero-order hold (ZOH) [1] and {2} the active control law for CSD. After receiving the active control law, the controller block in this system calculates the displacement of the activating bar or producing a semi-active control force. In other words, it is an active control force that decides how a hybrid controllable structure responses. Figure 4 depicts the block diagram of a system controlled by the (VFD+CSD). The Closed-loop feedback control is used in this paper, and thus the active-controlled force matrix can be expressed as:  $\hat{\mathbf{u}}(t) = -\mathbf{F} \cdot \mathbf{z}(t)$  (8), here  $\mathbf{F}$  is a matrix of feedback gain. Four algorithms to determine the matrix  $\mathbf{F}$  are exhibited in the following subsections.

### II.3. Determining the Active Feedback Gain [1]

#### II.3.1. Riccati Optimal Active Control Algorithm (ROAC)

In the Riccati optimal algorithm, the control force  $\hat{\mathbf{u}}(t)$  may be determined by minimizing a standard quadratic index  $J$ , given by:  $J = \frac{1}{2} \int_{t_0}^{t_f} [\mathbf{z}(t)^T \mathbf{Q} \mathbf{z}(t) + \hat{\mathbf{u}}(t)^T \mathbf{R} \hat{\mathbf{u}}(t)] dt$  (9), where  $\mathbf{Q}$  is a positive semi-definite symmetrical matrix;  $\mathbf{R}$  is a positive-definite symmetrical matrix so that all control forces are effective; performance index,  $J$ , represents a weighted balance between structural response and control energy. According to mechanic meaning,  $J$  is the energy the structure consumes during the earthquake period.

In accordance with [1], the Riccati equation:  $\mathbf{P}\mathbf{A} + \mathbf{A}^T \mathbf{P} - \mathbf{P}\mathbf{B}\mathbf{R}^{-1}\mathbf{B}^T \mathbf{P} + \mathbf{Q} = 0$  (10), Riccati matrix  $\mathbf{P}$  in this equation is constant and can be easily solved by numerical methods. Then, the active control expressed by equation (8) becomes:  $\hat{\mathbf{u}}(t) = -\mathbf{R}^{-1}\mathbf{B}^T \mathbf{P} \mathbf{z}(t) = -\mathbf{F} \mathbf{z}(t)$  (11), where  $\mathbf{F} = \mathbf{R}^{-1}\mathbf{B}^T \mathbf{P}$  (12)

#### II.3.2. Instantaneous Control with Displacement and Velocity Feedback (ICDVF)

The feedback gain is given in a concise matrix form  $\mathbf{F} = \mathbf{B}_2^{-1} [\mathbf{\Phi}_{2c} \cdot \text{diag}(\lambda_i)_c - \mathbf{A}_2 \cdot \mathbf{\Phi}_c] \cdot (\mathbf{C}_c \cdot \mathbf{\Phi}_c)^{-1}$  (13), where the diagonal matrix  $\text{diag}(\lambda_i)_c$  and the rectangular matrix  $\mathbf{\Phi}_c$  contain the target eigenvalues and eigenvectors, respectively. The matrices  $\mathbf{A}_2$ ,  $\mathbf{B}_2$  and  $\mathbf{\Phi}_{2c}$  are the lower portions of the matrices  $\mathbf{A}$ ,  $\mathbf{B}$ , and  $\mathbf{\Phi}_c$ ;  $\mathbf{C}_c$  denotes the sensor placement matrix.

#### II.3.3. Instantaneous Optimal Active Closed-Loop Control Algorithm (IOAC)

In the IOAC algorithm, the optimal control force  $\mathbf{u}(t)$  is determined by minimizing an instantaneous time-dependent performance index  $J_p(t)$  rather than ROAC integral performance index  $J$ :  $J_p(t) = \mathbf{z}(t)^T \mathbf{Q} \mathbf{z}(t) + \hat{\mathbf{u}}(t)^T \mathbf{R} \hat{\mathbf{u}}(t)$  (14)

The optimal control force  $\hat{\mathbf{u}}(t)$  depends on the time interval  $\Delta t$   $t_0 \leq t \leq t_f$  and is given by:

$$\hat{\mathbf{u}}(t) = -\left(\frac{\Delta t}{2}\right) \mathbf{R}^{-1} \mathbf{B}^T \mathbf{Q} \mathbf{z}(t) = -\mathbf{F} \mathbf{z}(t) \quad (15), \text{ where } \mathbf{F} = \left(\frac{\Delta t}{2}\right) \mathbf{R}^{-1} \mathbf{B}^T \mathbf{Q} \quad (16)$$

#### II.3.4. Pole Placement Algorithm

$\mathbf{F}$  is determined from solving the following equation:  $|s\mathbf{I} - \mathbf{A} + \mathbf{B}\mathbf{F}| = (s - s_1)(s - s_2) \dots (s - s_n)$  (17), where  $s_i (i = 1, 2, \dots, n)$  is chosen to be eigenvalues of matrix  $\mathbf{A}$ ;  $\mathbf{F}$  is chosen so that  $|\mathbf{A} - \mathbf{B}\mathbf{F}|$  having its eigenvalues will be  $s_i$

## III. NUMERICAL EXAMPLES

The 20-story structure used for this benchmark study was designed by Brandow and Johnston Associates in 1996 for the SAC Phase II Steel Project [4]. These buildings were chosen because they also serve as benchmark structures for the SAC studies and, thus, will provide a wider basis for comparing results. All simulations were performed by using routines written in MATLAB.

### III.1. Description of the 20-story benchmark structure

The 20-story structure is made of steel with  $E = 200\text{GPa}$ . The modal damping ratios of the steel frame are  $\zeta = 2\%$ . The dynamic properties of structure are given in Table 1.

Table 1. The dynamic properties of the 20-story structure

$i^{th}$ Floor	1 <sup>st</sup>	2 <sup>nd</sup> -4 <sup>th</sup>	5 <sup>th</sup> -10 <sup>th</sup>	11 <sup>th</sup> -13 <sup>th</sup>	14 <sup>th</sup> -16 <sup>th</sup>	17 <sup>th</sup> -18 <sup>th</sup>	19 <sup>th</sup>	20 <sup>th</sup>
$k_i$ (kN/cm)	30173	80400	51686	42295	27160	23917	16012	16012
$m_i$ ( $\times 10^3$ kg)	563	552	552	552	552	552	552	584

When the smart structure is not controlled, the first three natural frequencies corresponding to the first three modes are  $\omega_1 = 7.1\text{rad/s}$ ;  $\omega_2 = 18.2\text{rad/s}$ ;  $\omega_3 = 30.3\text{rad/s}$ . The first three-time period of the structure are  $T_1 = 0.88\text{sec}$ ;  $T_2 = 0.34\text{sec}$ ;  $T_3 = 0.21\text{sec}$ . The viscous dampers coefficients of VFD (passive control) [3]:  $C_i^{VFD} = 1.2 \times 10^3$  (kN.s/cm). For CSD and from the Century Spring manufacture, the stiffness values of mainsprings of CSD (semi-active control) are taken as the maximum value of  $C_i^M$  and  $x_{\text{limit},i}^{t \text{ or } c}$  [3]:  $C_i^M = 46.62$  (kN/cm).  $x_{\text{limit},i}^{t \text{ or } c} = 7.5$  (cm). The response of the 20-story structure is computed for Northridge seismic excitation.

III.2. The dynamic response and the reductions of the structure using four algorithms

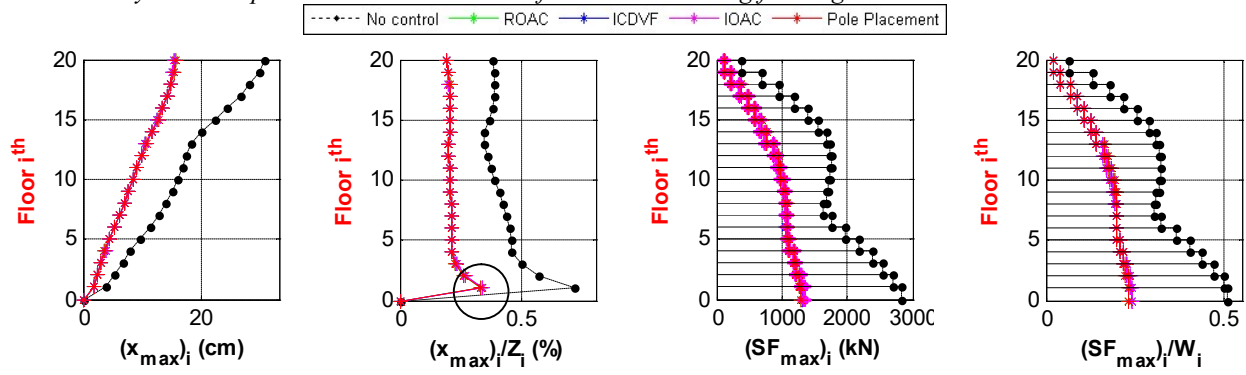


Figure 5. The maximum displacement response at the floors

Figure 6. The maximum shear force response relative to the height at the floors

Figure 7. The maximum shear force response at the floors

Figure 8. The maximum shear force response relative to the weight at the floors

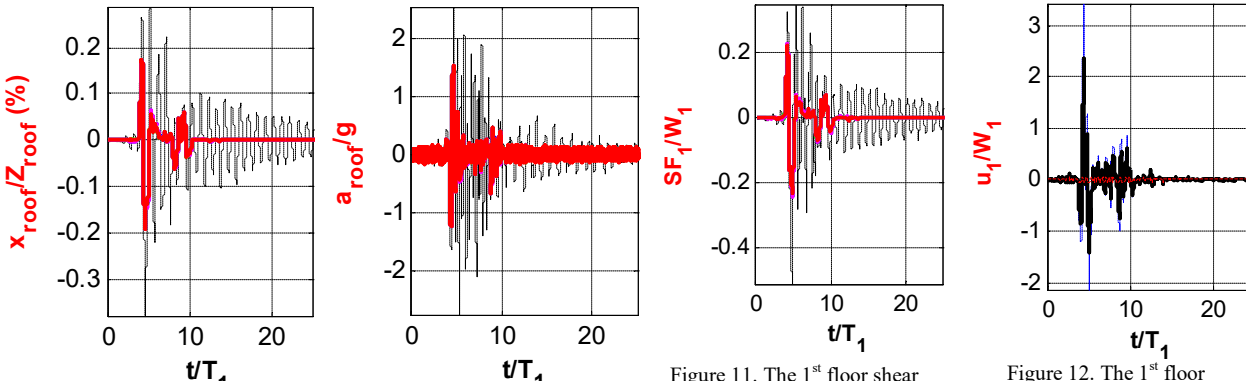
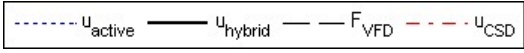


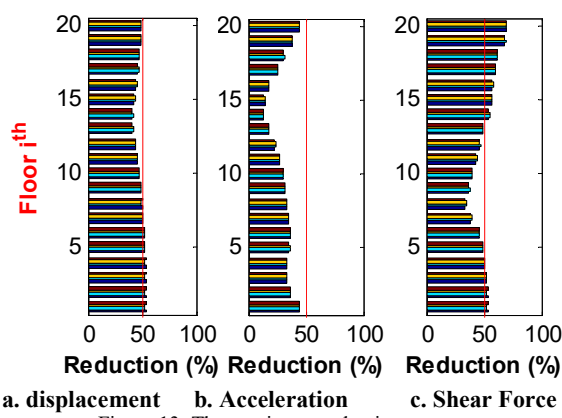
Figure 9. The roof displacement time history

Figure 10. The roof acceleration time history

Figure 11. The 1<sup>st</sup> floor shear force time history

Figure 12. The 1<sup>st</sup> floor controlled force time history with IOAC





a. displacement b. Acceleration c. Shear Force  
Figure 13. The maximum reduction

Whereas without the dampers, this ratio is 0.29% and exceeds the allowance value. Additionally, the hybrid structural control also reduces the 1<sup>st</sup> floor's deviation ( $(x_{\max})_1/Z_1$ ) (Figure 6), which is the main reason for the collapse of the building. Without using a damper, the column's stiffness at the 1<sup>st</sup> floor is enhanced up to 4 times to resist structural responses.

For this reason, hybrid control is appropriate to improve the seismic resistance of used buildings which must meet the requirements of seismic design's Vietnam code. Nevertheless, the maximum ratio of  $a_{\text{roof}}$  to  $g$  (the gravity acceleration, take  $9.81\text{m/s}^2$ ) of the hybrid structure is equal to 1.53 and larger than the Vietnam standard ratio of 0.1. Ultimately, the hybrid control does not satisfy the impulse of the active control force (due to the capacity in generating control force of both VFD and CSD) (Figure 12), but the maximum reduction is approximately 50%.

### III.3. The effectiveness of the response reduction of the hybrid control structure with only VFD and CSD

The response of the 20-story building under the seismic excitations is checked for the following five cases such as (A) uncontrolled structure; (B) passive control only VFD of  $C_i^{\text{VFD}} = 1.2 \times 10^3 \text{ (kN.s/cm)}$ ; (C) semi-active control only CSD of  $C_i^M = 46.62 \text{ (kN/cm)}$  and  $x_{\text{limit},i}^{\text{or } c} = 7.5 \text{ (cm)}$  using IOAC; (D) hybrid control both the VFD and CSD with IOAC.

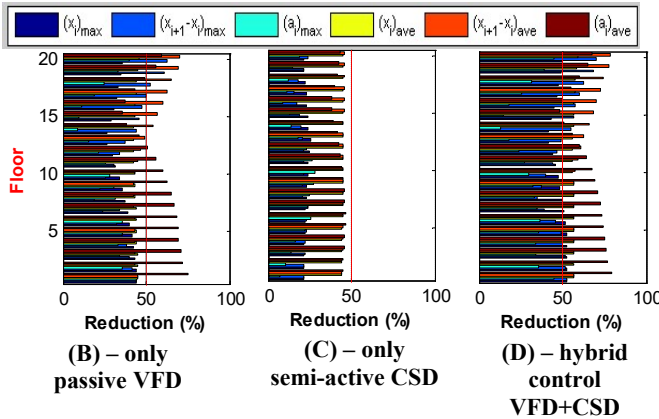


Figure 14. The response reduction of the structure

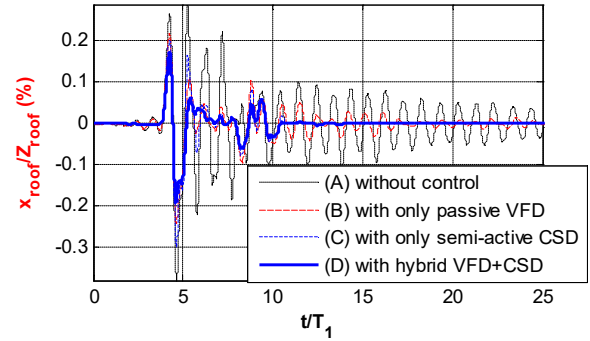


Figure 15: The roof displacement time history at the top floor

The criteria in attempts to assess the effectiveness in these cases (B), (C), and (D) is the response reduction

$$R_{\text{mean}} \text{ and is computed by } R_{\text{mean}} = \frac{2 \times R_{\text{max}}^{\text{mean}} + R_{\text{ave}}^{\text{mean}}}{3} \quad (18), \quad \text{where} \quad R_{\text{max ave}}^{\text{mean}} = \frac{1}{n} \sum_{i=1}^{n=20} \left[ R_{(x_i)_{\text{max ave}}} + R_{(x_{i+1}-x_i)_{\text{max ave}}} + R_{(a_i)_{\text{max ave}}} \right];$$

$R_{(x_i)_{\text{max ave}}}$ ,  $R_{(x_{i+1}-x_i)_{\text{max ave}}}$ , and  $R_{(a_i)_{\text{max ave}}}$  is the maximum and average displacement, relative displacement, and acceleration reductions compared with the no control case at the floors, respectively. The average responses are calculated with the root-mean square value. The significance of the maximum response is taken into account in the expression (18) with the scale factor of 2.

Table 2: The response reduction in three cases (B), (C), (D)

CASE	$\frac{1}{n} \sum_{i=1}^{n=20} R_{(x_i)_{\max}}$	$\frac{1}{n} \sum_{i=1}^{n=20} R_{(x_{i+1}-x_i)_{\max}}$	$\frac{1}{n} \sum_{i=1}^{n=20} R_{(a_i)_{\max}}$	$R_{\max}^{\text{mean}}$
<b>(B)</b>	35.6%	39.5%	27.7%	<b>34.2%</b>
<b>(C)</b>	22.9%	20.9%	18.0%	<b>20.6%</b>
<b>(D)</b>	48.3%	51.2%	30.4%	<b>43.3%</b>
	$\frac{1}{n} \sum_{i=1}^{n=20} R_{(x_i)_{\text{ave}}}$	$\frac{1}{n} \sum_{i=1}^{n=20} R_{(x_{i+1}-x_i)_{\text{ave}}}$	$\frac{1}{n} \sum_{i=1}^{n=20} R_{(a_i)_{\text{ave}}}$	$R_{\text{ave}}^{\text{mean}}$
<b>(B)</b>	43.8%	50.7%	57.6%	<b>50.7%</b>
<b>(C)</b>	44.8%	45.3%	43.3%	<b>44.5%</b>
<b>(D)</b>	56.9%	62.8%	65.7%	<b>61.8%</b>

Among these cases, case (D) gives the best reduction  $R_{\text{mean}} = 49.5\%$ , case (B) has  $R_{\text{mean}} = 39.7\%$ , and case (C) has  $R_{\text{mean}} = 28.6\%$  (Table 2).  $R_{\text{mean}}$  of the case (B) (passive control) is even larger than that of case (C) (semi-active control). This results from the small capability of both  $C_i^M$  and  $x_{i\text{limit},i}$  is used with the maximum values. CSDs are therefore not able to produce a significant control force to reduce the structural responses. In order to increase the response reduction, the number of CSD used in the structure should be adequate to the demand for a semi-active control force. Also, the CSD is very useful to eliminate the small vibration from  $t/T_1 = 12$  to 25 (Figure 15), and this is not true in case (B). Lastly, for the smart structure, the combination of VFD and CSD {1} utilizes VFD's capability for generating control force to make up for the lack of CSD's semi-active control force and (2) dismisses the small vibration phrase.

#### II.4. The effectiveness of response reductions of the hybrid structure with the classical solution

For the effectiveness of response reductions of the structure, simulations were carried out on two solutions consisting of (D) using the hybrid control (VFD+CSD) and (E) four times of increasing the column's stiffness of structure (the stiffness of floors is calculated with (5))

Table 3. Column section property type of each solution, wide flange section

$i^{\text{th}}$ floor	Solution (D)		Solution (E)	
	property type	Section A (cm <sup>2</sup> )	property type	Section A (cm <sup>2</sup> )
1	W24x335	634.8	W36x848	1,225.8
2	W24x335	634.8	W36x848	1,225.8
3	W24x335	634.8	W36x848	1,225.8
4	W24x335	634.8	W36x848	1,225.8
5	W24x229	433.5	W30x526	993.5
6	W24x229	433.5	W30x526	993.5
7	W24x229	433.5	W30x526	993.5
8	W24x229	433.5	W30x526	993.5
9	W24x229	433.5	W30x526	993.5
10	W24x229	433.5	W30x526	993.5
11	W24x192	363.2	W27x539	1,019.4
12	W24x192	363.2	W27x539	1,019.4
13	W24x192	363.2	W27x539	1,019.4
14	W24x131	248.4	W24x450	851.6
15	W24x131	248.4	W24x450	851.6
16	W24x131	248.4	W24x450	851.6
17	W24x117	221.9	W24x408	767.7
18	W24x117	221.9	W24x408	767.7
19	W24x84	159.4	W24x279	529.0
20	W24x84	159.4	W24x279	529.0
		<b>7,737.6</b>		<b>19,070.6</b>



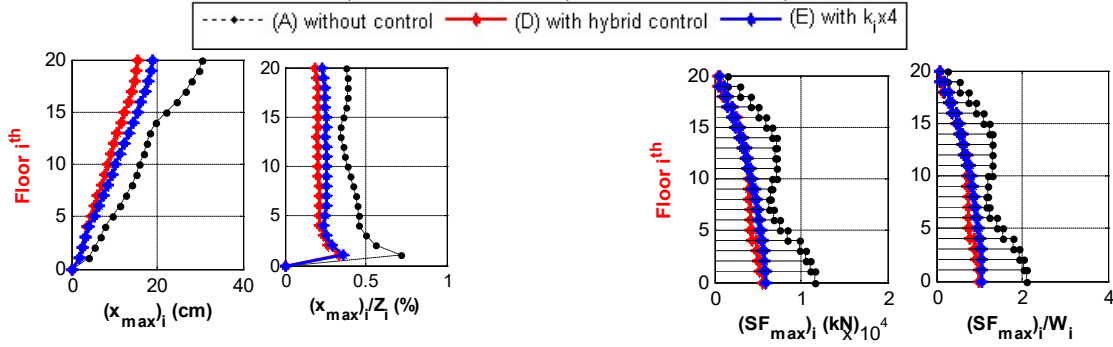


Figure 16. The maximum displacement response at the floors

Figure 17. The maximum shear force response at the floors

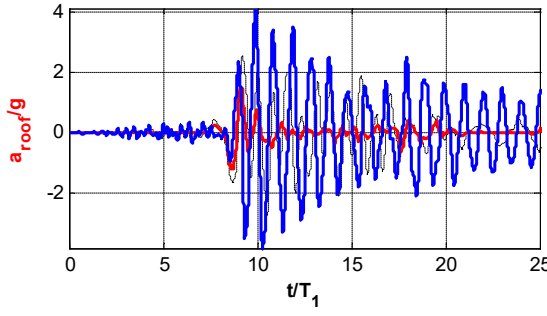


Figure 18. The roof acceleration time history

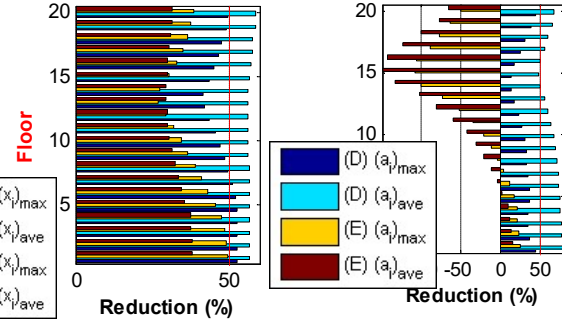


Figure 19. The maximum displacement reduction

Figure 20. The maximum acceleration reduction

As the columns' stiffness of the structure increase four times, the displacement is also enhanced, corresponding to the column's stiffness (Figure 16 and Figure 19). However, the acceleration response reduction is negative (Figure 20), i.e., causing higher acceleration because the structure becomes stocky. Additionally, the maximum shear force responses of (D) and (E) are nearly familiar (Figure 17), but in order to get the amount of the reduction, the columns' stiffness of the structure in the case (E) must be four times increase. That means the steel material used for this building must upgrade, up to  $\frac{19,070.6}{7,737.6} = 2.46$  times, i.e., the costs for the material are lessened by approximately 59.4 percent when the structure uses the hybrid controlled system.

#### IV. CONCLUSION

As a hybrid control system, the 20-story structure is either the passive control with VFD or the semi-active control with CSD. Therefore, the hybrid control system with (VFD+CSD) is suitable for various kinds of seismic loadings. Furthermore, when CSD uses an active control algorithm for the controller, this paper shows that all of the four active algorithms give almost the same responses. As structures are equipped with (VFD+CSD), the energy dissipation of the system is principally the task of VFD. Yet, with the same mainspring stiffness and CSD used as semi-active control devices, the response reduction develops effectiveness. The article also displays that the hybrid control system in the 20-story building has more advantages for the seismic resistance than a traditional solution, such as lowering a significant amount of the material or not increasing the acceleration response for the structure. Besides, this research introduces an option for structural control, the hybrid control. To lessen costly consumption during operation and maintenance of using CSD and VFD simultaneously but the structure obtains desired effectiveness, the hybrid control system (VFD+CSD) is one of the optimal choices. Eventually, a hybrid control system with (VFD+CSD) in high-rise building becomes suitable for Vietnam condition being on the medium earthquake domain.

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